

# Ocean Constraints on the Atmospheric Inverse Problem: The contribution of Forward and Inverse Models

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## *Acknowledgements*

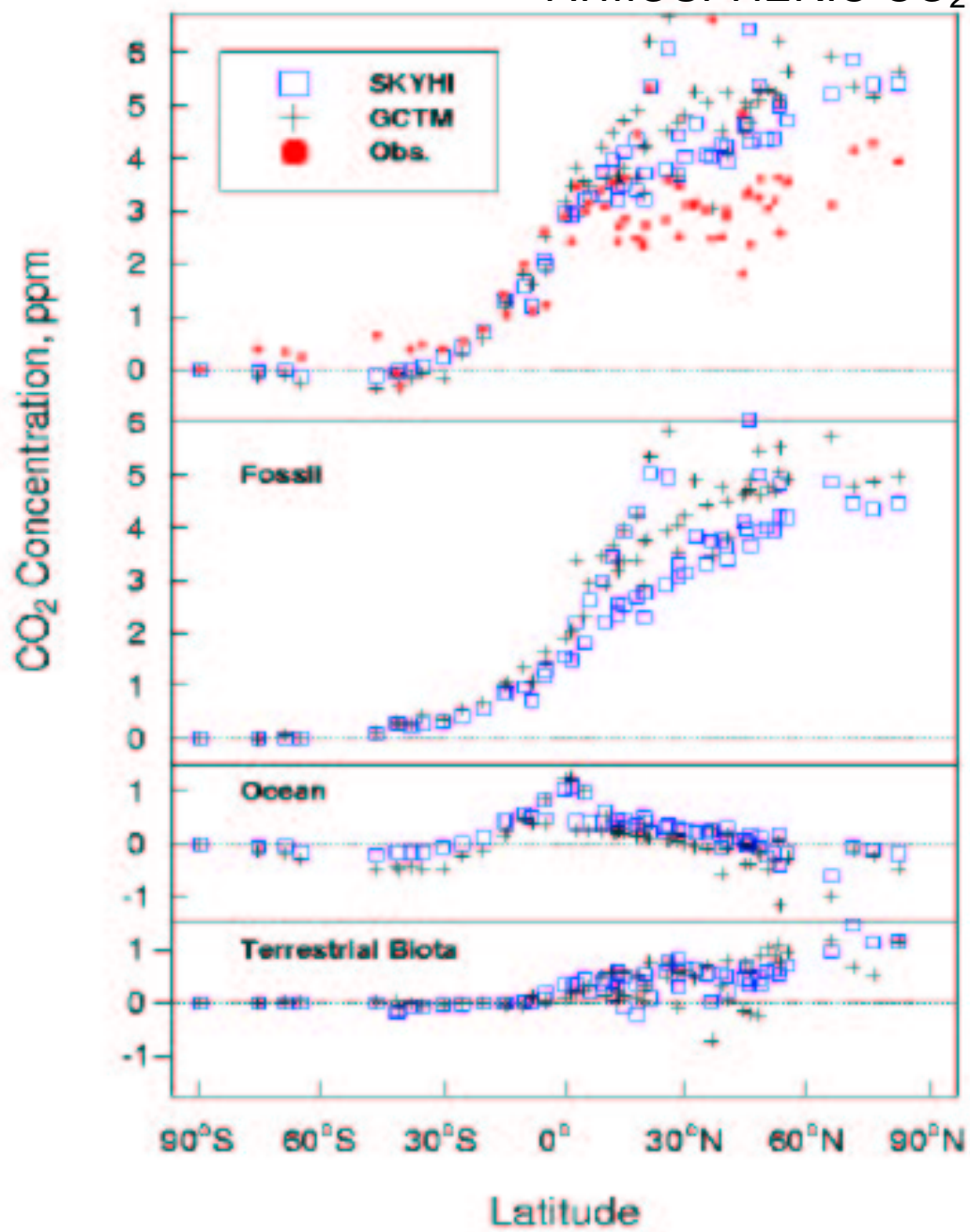
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J. C. Orr<sup>5</sup> and the OCMIP members

- (1) Max Planck Institute for Biogeochemistry, Jena, Germany
- (2) Program in Oceanic and Atmospheric Sciences, Princeton University
- (3) JISAO, University of Washington, Seattle
- (4) Pacific Marine Environmental Laboratory, Seattle
- (5) Lab. des Sciences du Climat de l'Environnement, Gif-sur-Yvette, France

# Outline

1. Introduction: A short historical overview
2. Observational approaches
3. Forward Modeling
4. Inverse Modeling
5. Regionalization
6. Summary and Conclusion

## INTERHEMISPHERIC GRADIENT OF ATMOSPHERIC CO<sub>2</sub>

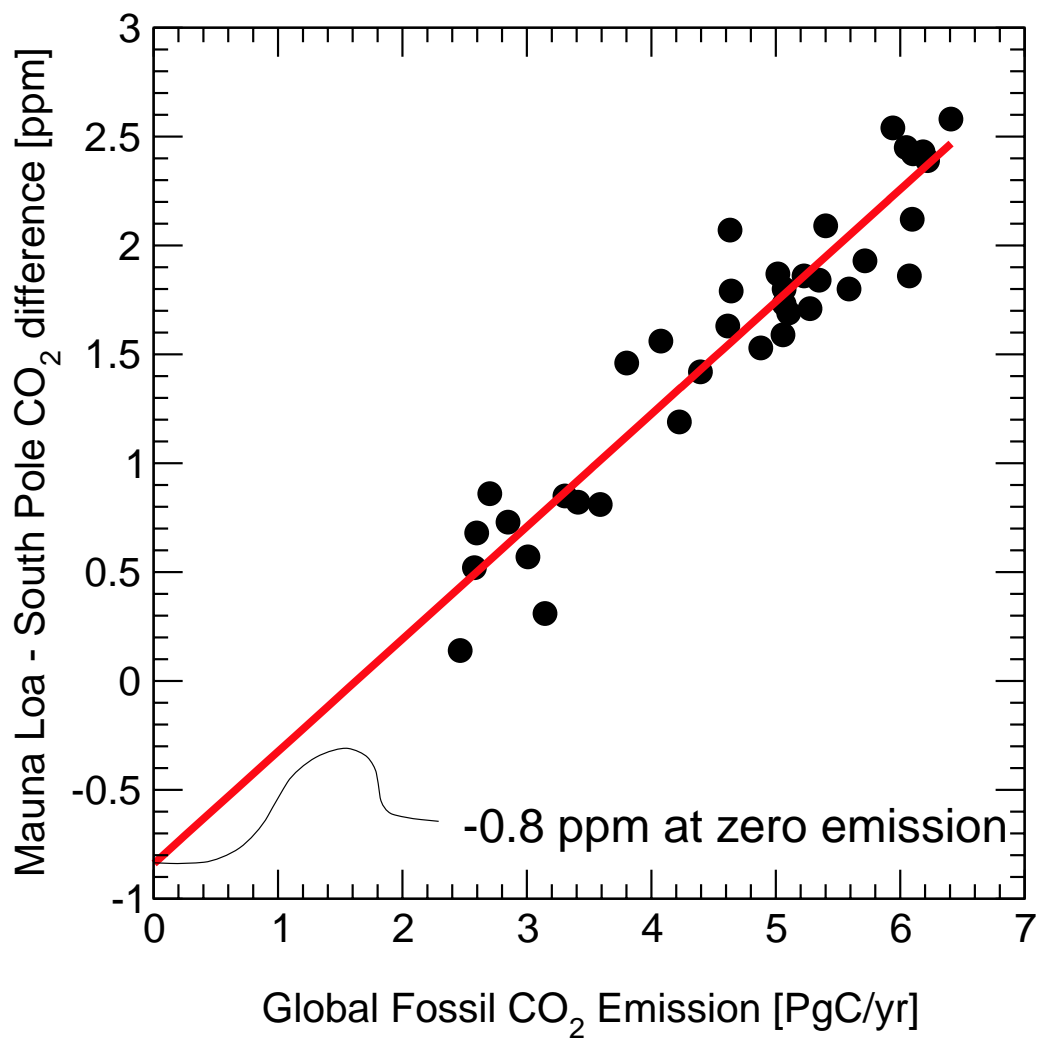


*Fan et al. (1999)*

# Interhemispheric ocean CO<sub>2</sub> transport

[*Keeling et al.*, 1989]

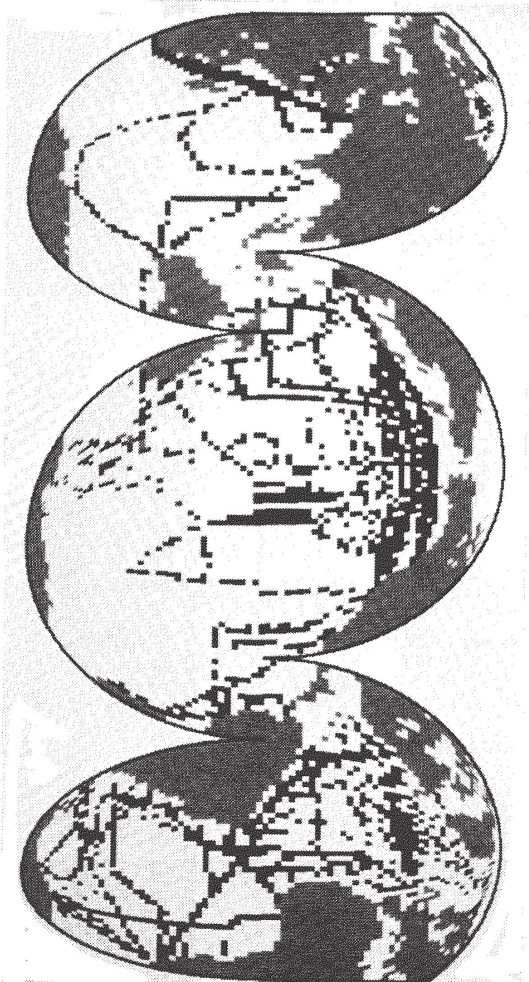
## PREINDUSTRIAL INTERHEMISPHERIC CO<sub>2</sub> GRADIENT



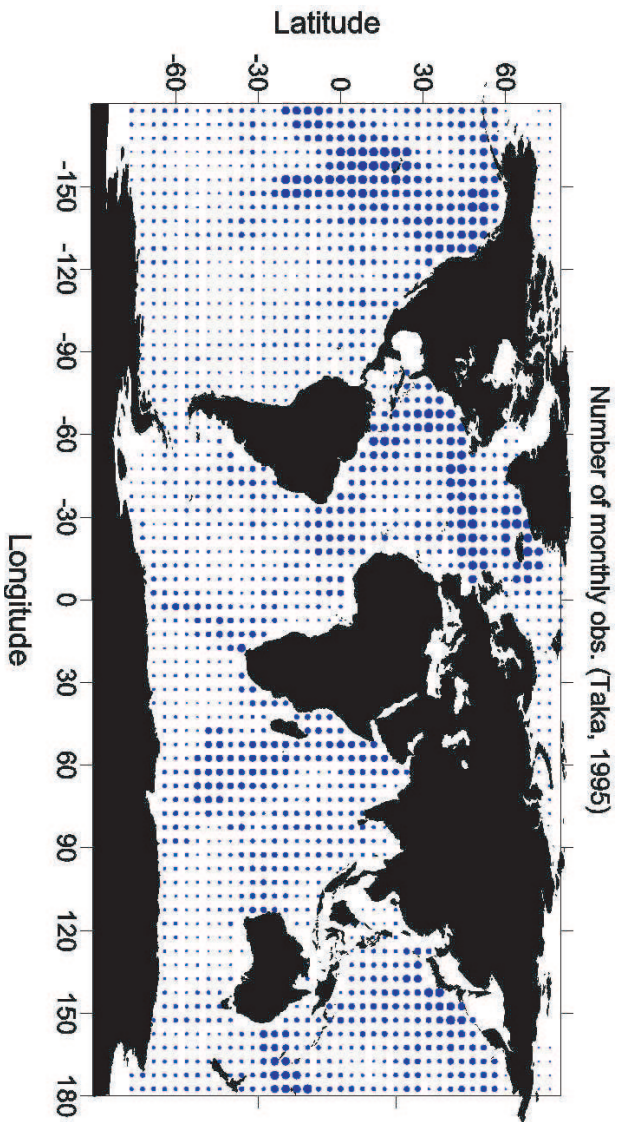
*adapted and updated from Keeling et al. (1989)*

# EVOLUTION OF OCEANIC pCO<sub>2</sub> NETWORK

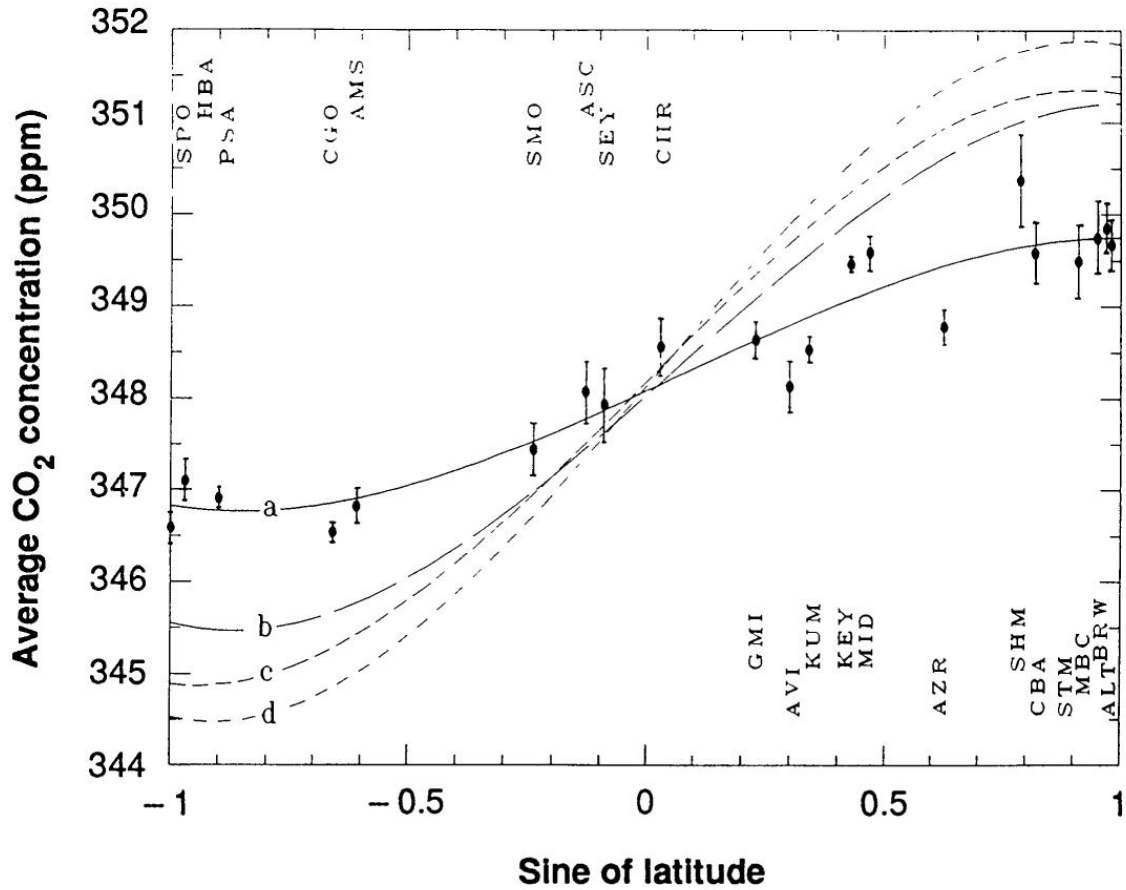
TANS ET AL. (1990)



TAKAHASHI ET AL. (1999)



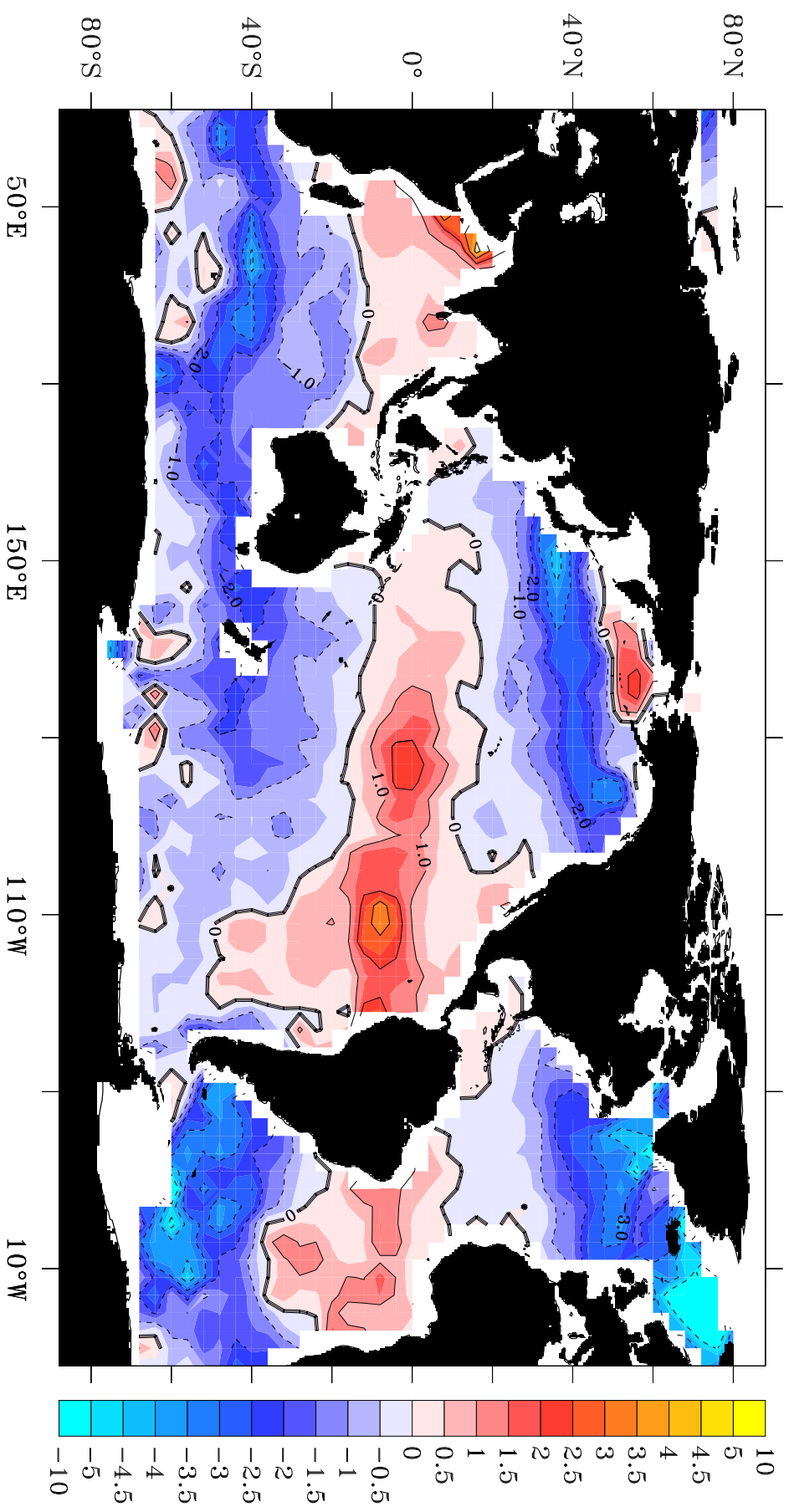
## OBSERVED AND PREDICTED ATMOSPHERIC CO<sub>2</sub>



*Tans et al. (1990)*

- a) fit to data
- b) predicted CO<sub>2</sub> concentration with fossil fuel emission, seasonal vegetation, tropical deforestation, and ocean flux computed using LM gas transfer coefficient
- c) as b, except for ocean flux computed using Tans et al. gas transfer coefficient
- d) as b, except for ocean flux computed using previous estimates

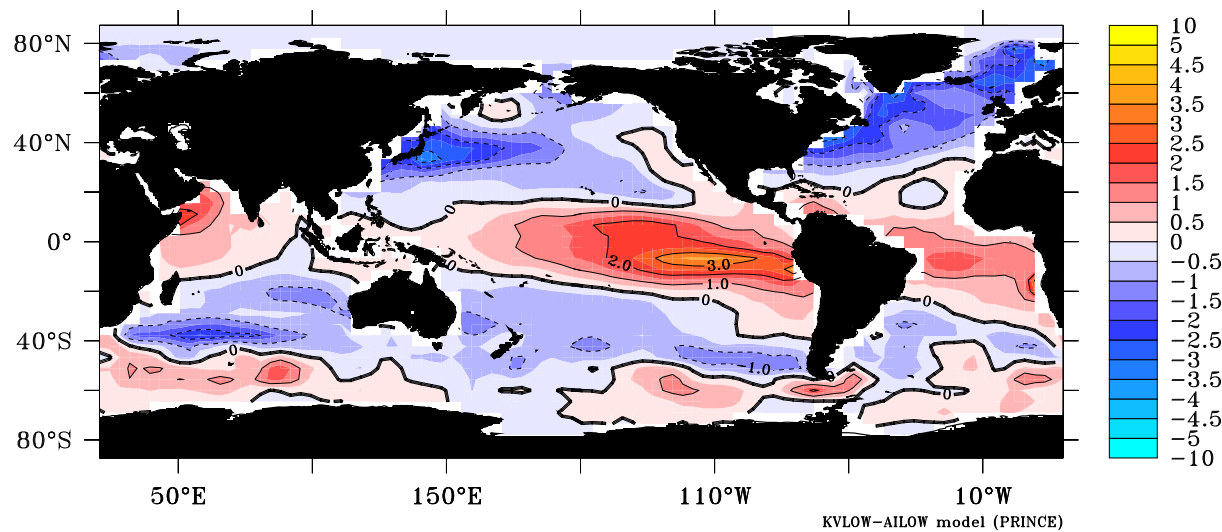
Annual CO<sub>2</sub> Flux (mol/m<sup>2</sup>/yr)



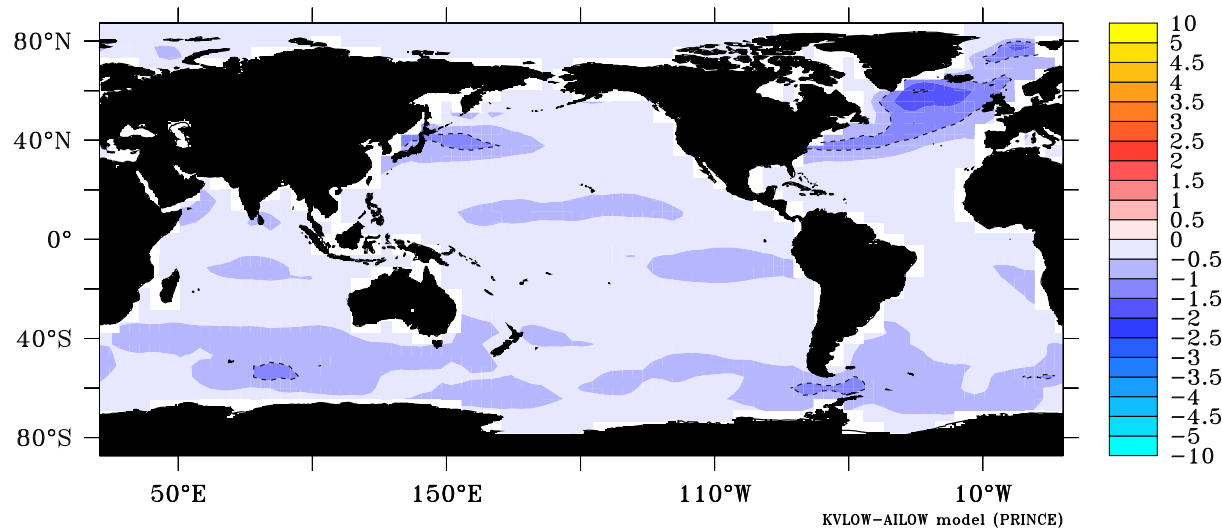
Takahashi et al. (2002)



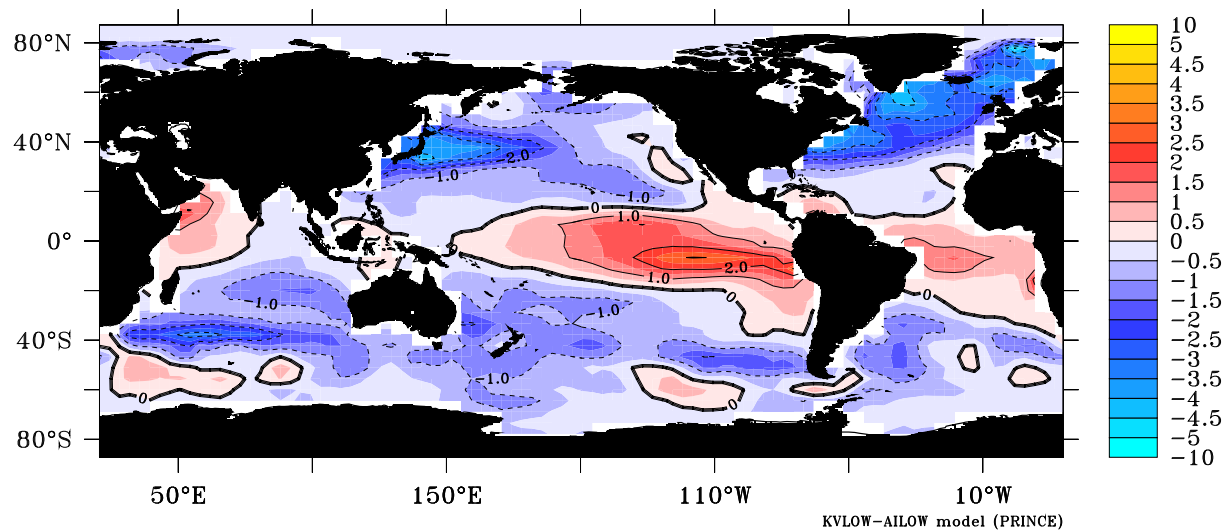
Pre-Industrial CO<sub>2</sub> Flux (mol/m<sup>2</sup>/yr)



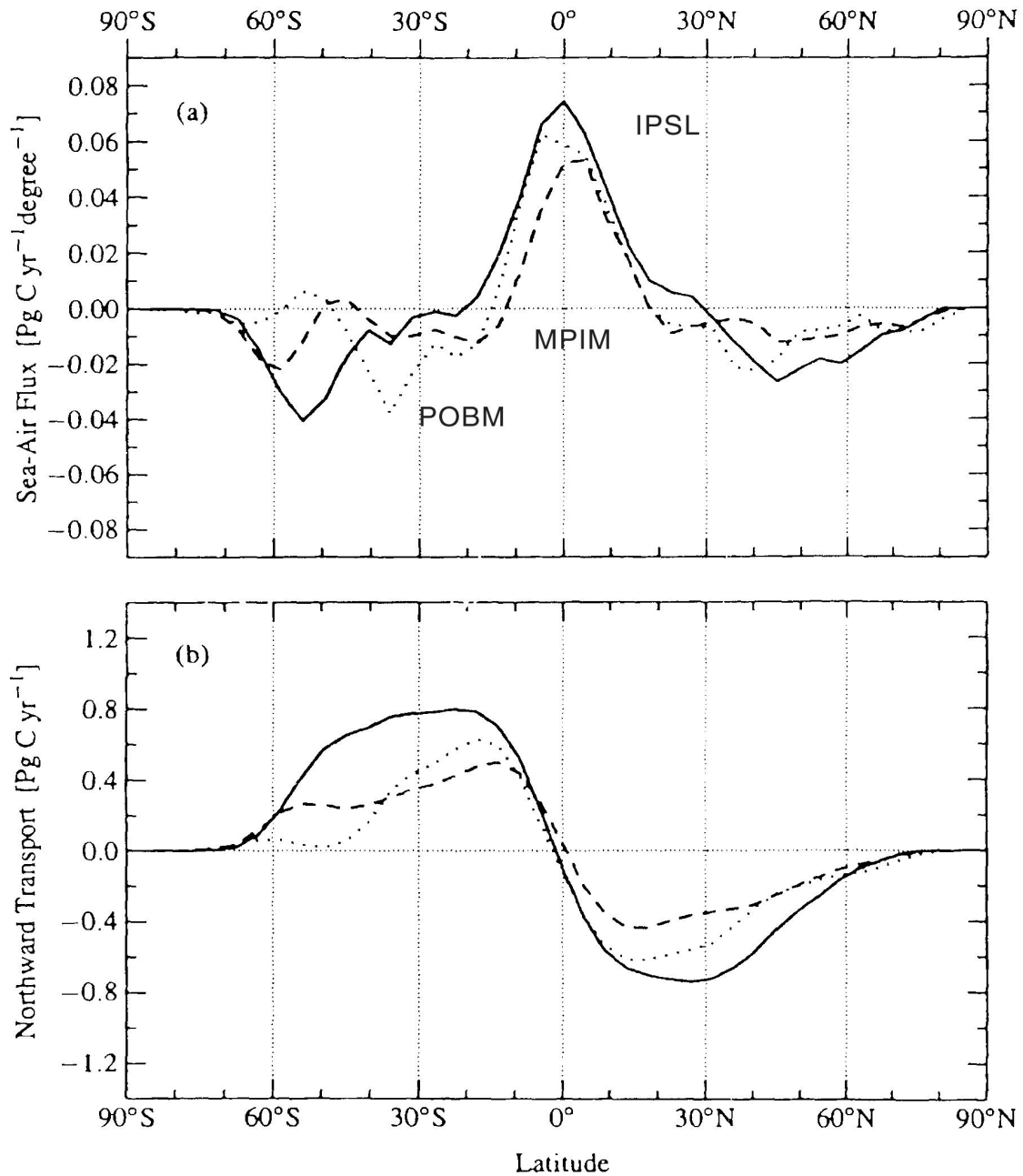
Anthropogenic CO<sub>2</sub> Flux (1990) (mol/m<sup>2</sup>/yr)



Contemporary CO<sub>2</sub> Flux (1990) (mol/m<sup>2</sup>/yr)

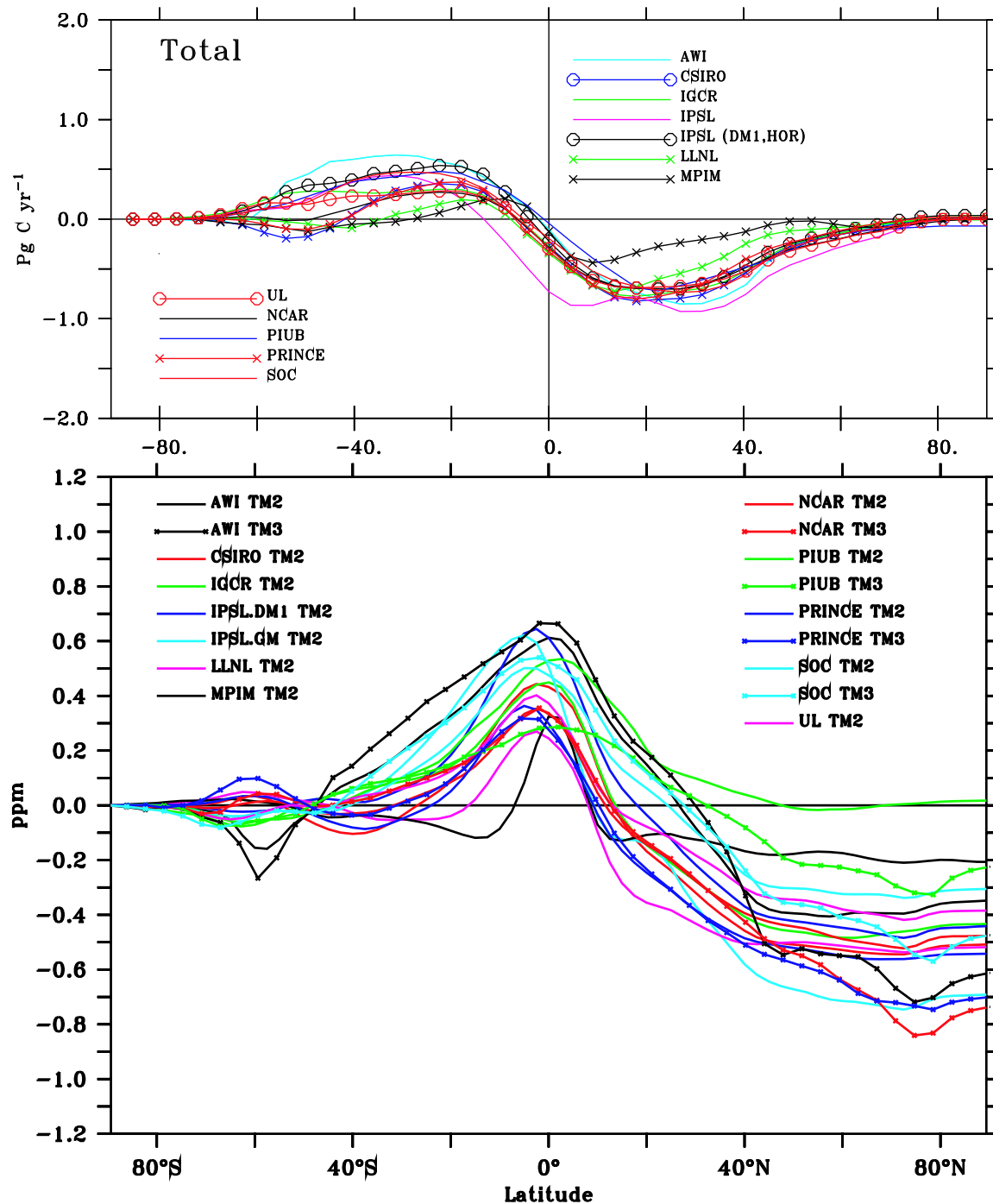


# OCMIP-1: CO<sub>2</sub> FLUXES AND OCEAN TRANSPORT



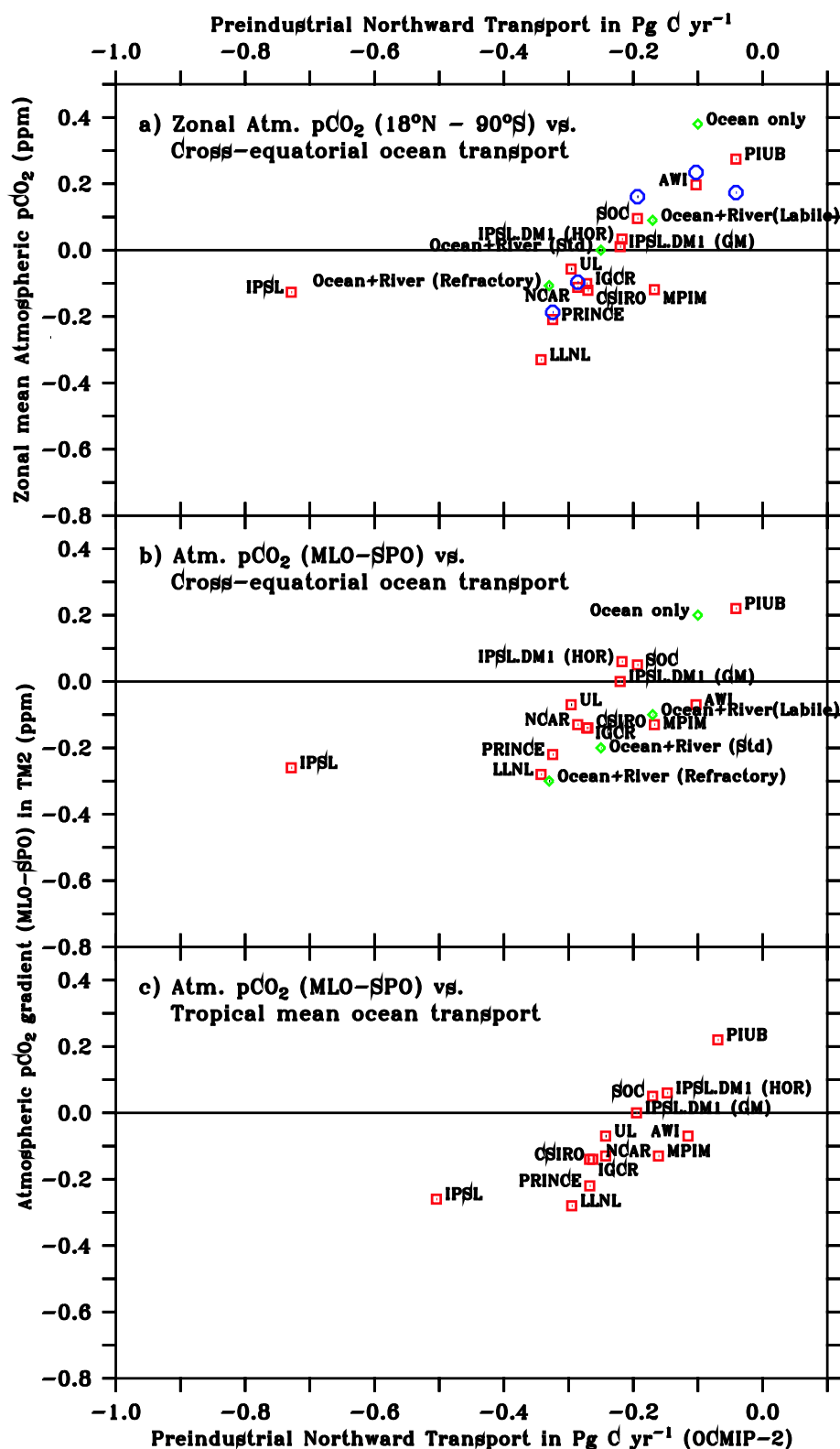
*Sarmiento et al. (2000)*

# OCMIP-2: OCEAN CO<sub>2</sub> TRANSPORTS AND ATM. RESPONSE

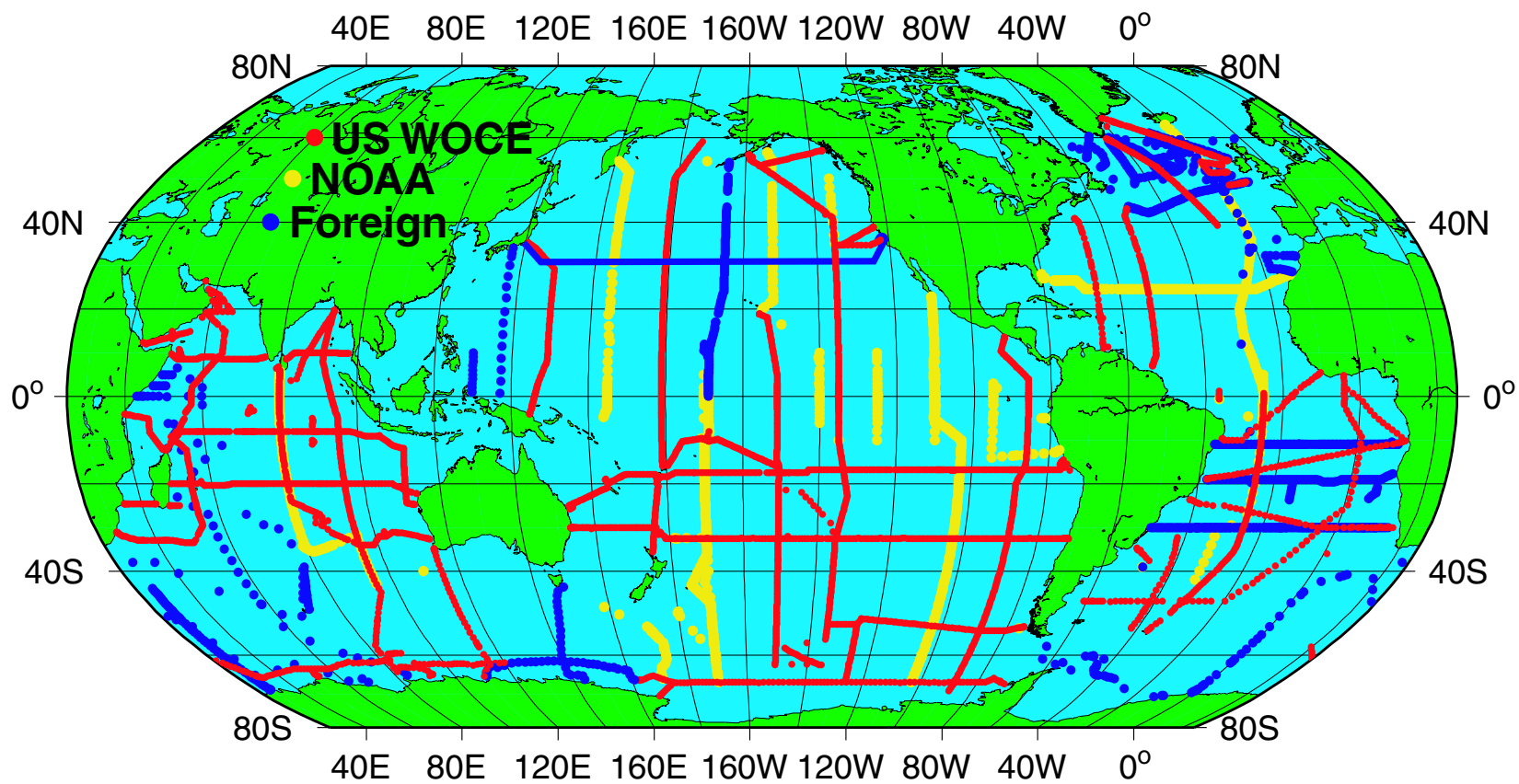


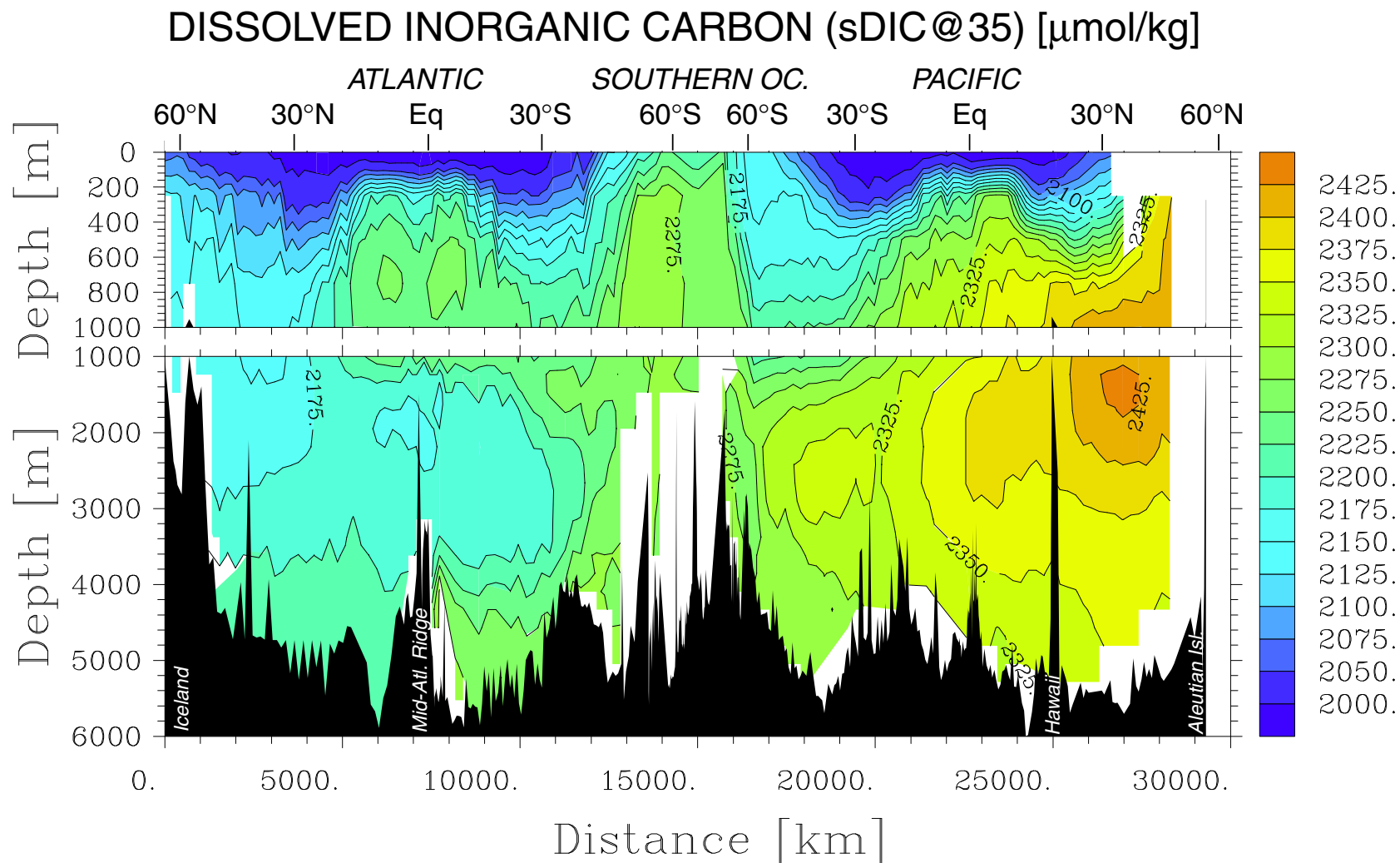
*J. Orr and OCMIP-2 (pers.comm)*

# OCMIP-2: OCEAN CO<sub>2</sub> TRANSPORT VERSUS ATMOSPHERIC GRADIENT



# WOCE/JGOFS CO<sub>2</sub> survey





What  $\Delta C_{\text{gas ex}}$  can tell us about the air-sea gas exchange of  $\text{CO}_2$

- Definition of  $\Delta C_{\text{gas ex}}$ :

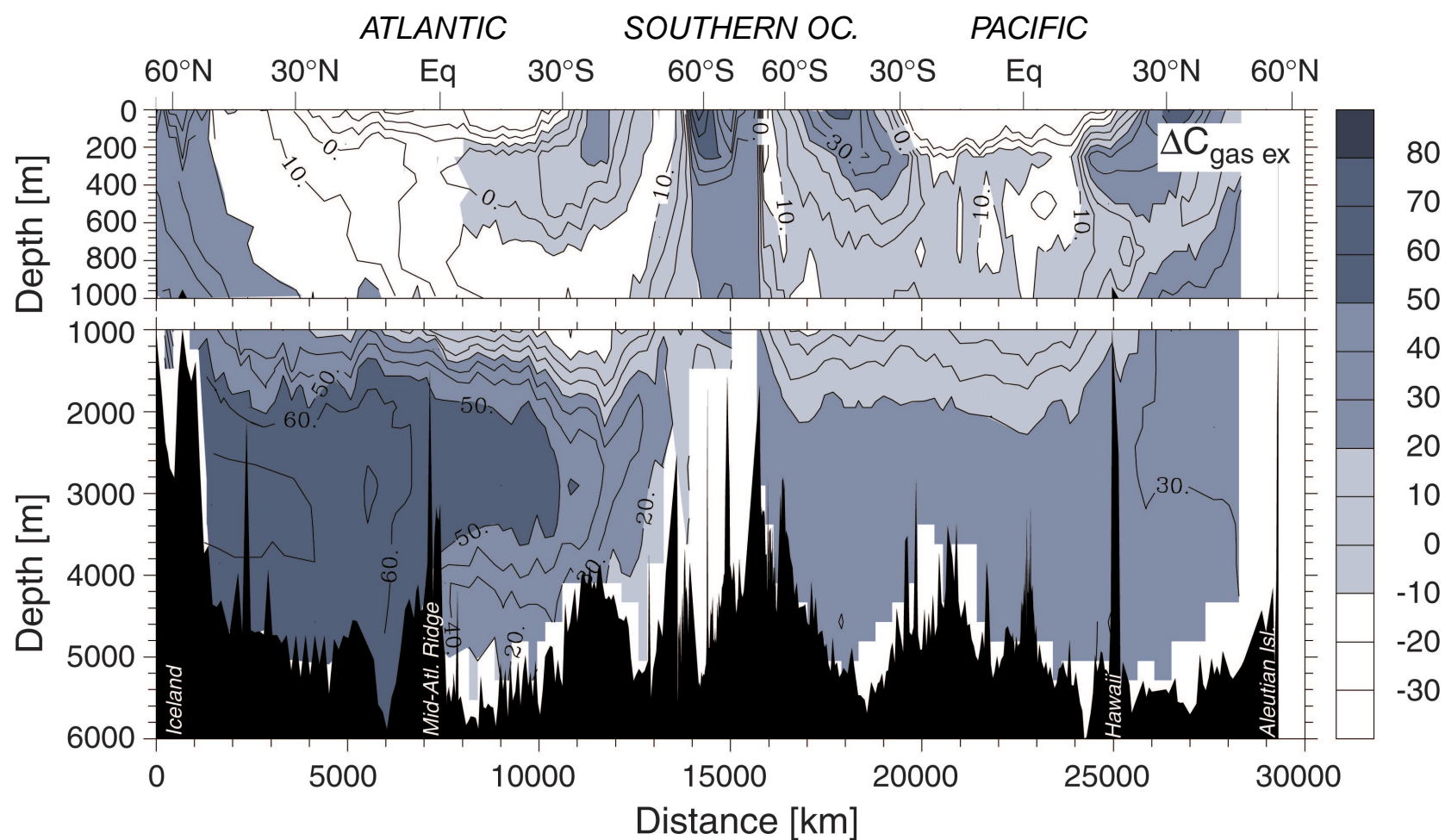
$$\Delta C_{\text{gas ex}} = \frac{S^o}{S} \left( DIC - r_{C:P}P - \frac{1}{2} (Alk + r_{N:P}P) \right) - \Delta C_{\text{ant}},$$

$$\Gamma(\Delta C_{\text{gas ex}}) = 0.$$

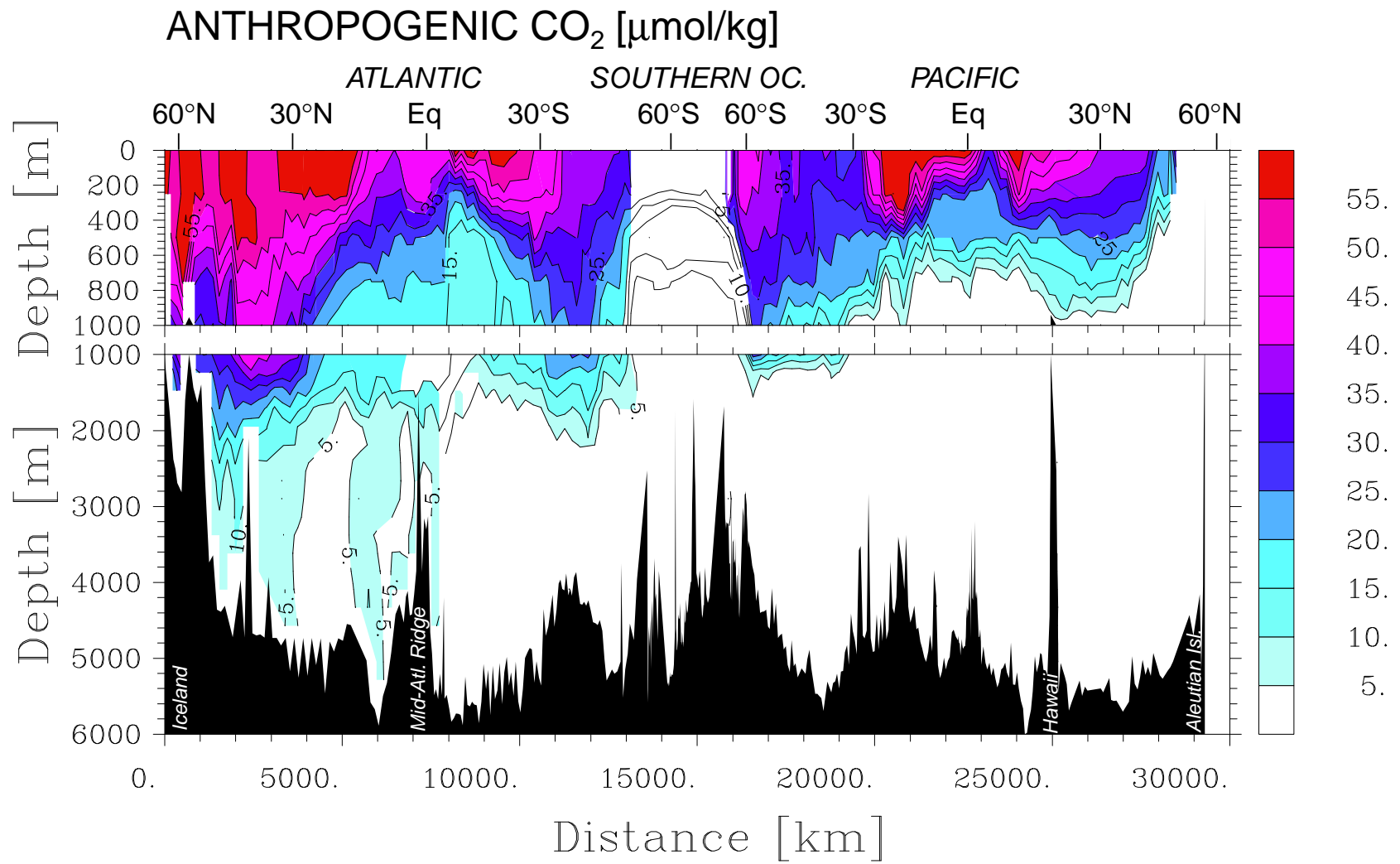
- Explanation and Interpretation :

- The normalization to constant Phosphate (P) and Alkalinity (Alk) removes the contribution of the soft-tissue and carbonate pumps.
- The remaining variability is due to the exchange of natural  $\text{CO}_2$  between the ocean and atmosphere as well as the uptake of anthropogenic  $\text{CO}_2$  ( $\Delta C_{\text{ant}}$ ).
- After removing  $\Delta C_{\text{ant}}$  as well, we end up with a tracer just reflecting the air-sea exchange of natural (i.e. pre-industrial)  $\text{CO}_2$ .

# GAS-EXCHANGE COMPONENT ( $\Delta C_{\text{gas-ex}}$ ) [ $\mu\text{mol/kg}$ ]







# Principle of Oceanic Inversion

- The ocean surface is partitioned into  $n$  regions.
- Basis functions

- *Steady-State Inversion*

In a OGCM, constant fluxes of dye tracers ( $\Phi$ ) are imposed in each of the  $n$  regions, and the model is run until the spatial patterns of the dyes attain a quasi steady-state.

- *Transient-tracer Inversion*

Analogous to the *steady-state* inversion except that the dye fluxes are time-varying, i.e. for  $\text{CO}_2$ ,

$$\vec{\Phi}(t) = \vec{\Phi}(t=0) * (p\text{CO}_2(t) - p\text{CO}_2(t=0))$$

- The model predictions of the dye concentrations are sampled at the observation stations and arranged as a vector  $\vec{\chi}_{\text{OGCM}}$ . The model therefore provides us with a transport matrix  $A_{\text{OGCM}}$  that relates the fluxes to the distribution,

$$\vec{\chi}_{\text{OGCM}} = A_{\text{OGCM}} \vec{\Phi}.$$

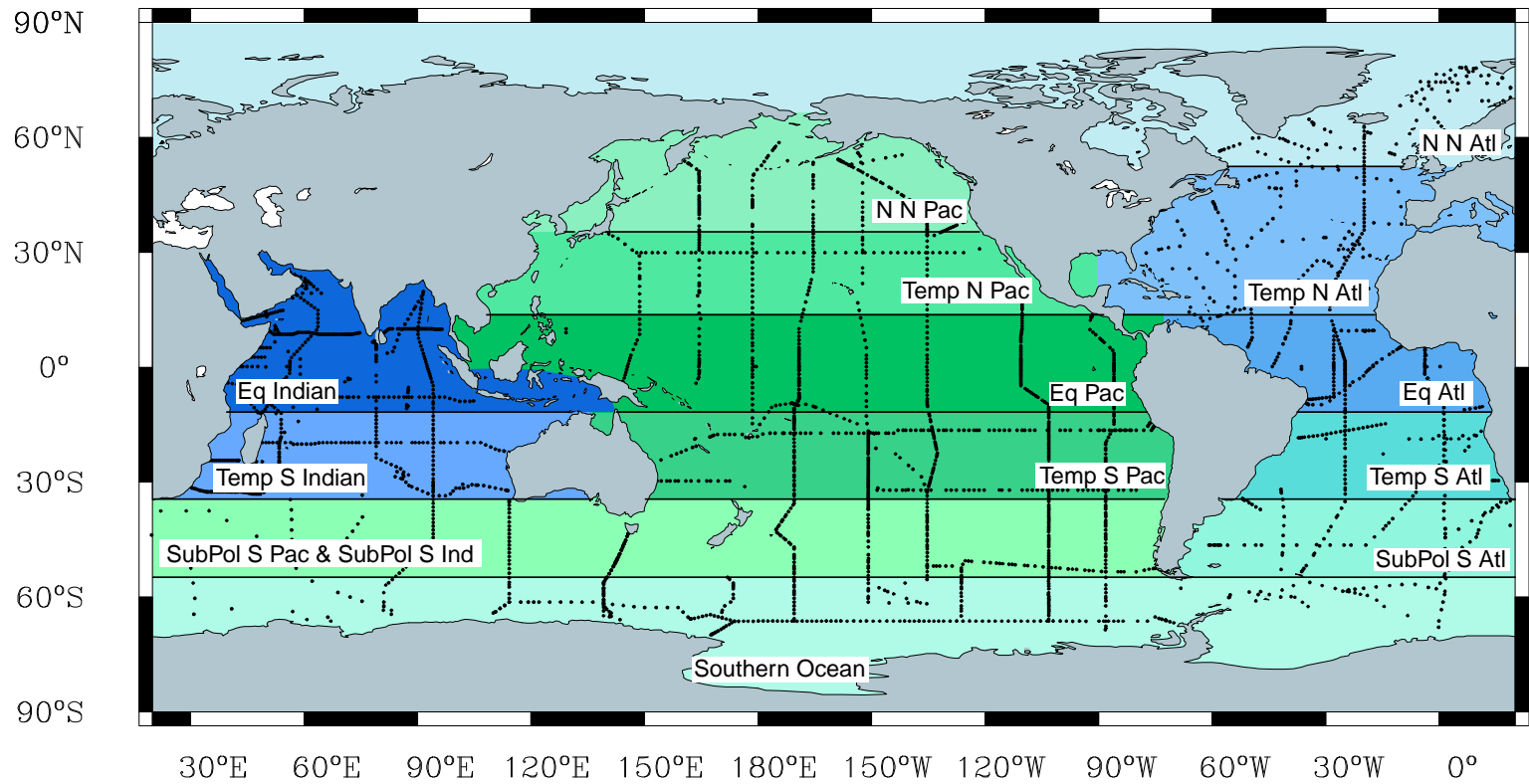
- Modeled distributions at the observations stations are substituted with observed ones and the matrix  $A$  is inverted to get an estimate of the surface fluxes ( $\vec{\Phi}_{\text{est}}$ ) :

$$\vec{\Phi}_{\text{est}} = A_{\text{OGCM}}^{-1} \vec{\chi}_{\text{obs}}.$$

## The Models

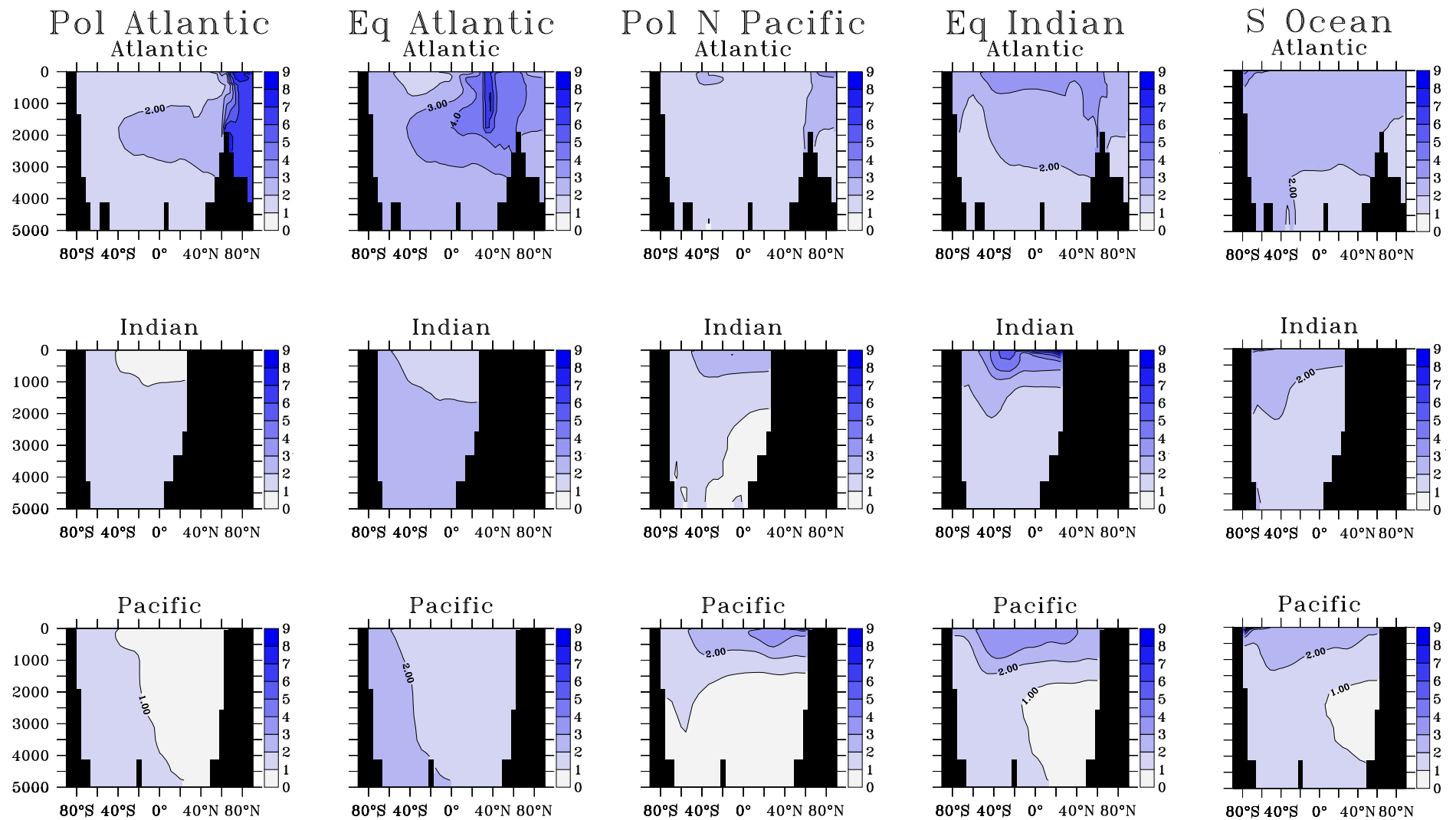
- coarse resolution model:  $3.75^\circ$  meridionally,  $4.5^\circ$  zonally and 24 layers vertically
- seasonal forcing at the surface with observed wind-stress, [Hellermann and Rosenstein, 1983] and heat and freshwater fluxes [DaSilva et al., 1994] with weak restoring towards observed temperature and salinity fields from Levitus et al. [1994].
- Sub-grid scale parameterization of eddies according to Gent and McWilliams [1990]
- KvLOW-AiLOW: Low vertical diffusivity everywhere; KvHISouth-AiLOW: Enhanced vertical diffusivity in the Southern Ocean.
- Surface ocean has been divided into 15 regions and unit fluxes have been applied for a total runtime of 3000 years. For the time-dependent inversion, the unit fluxes were scaled in time according to the evolution of the atmospheric  $\text{CO}_2$  perturbation.

# OCEAN REGIONS AND NETWORK

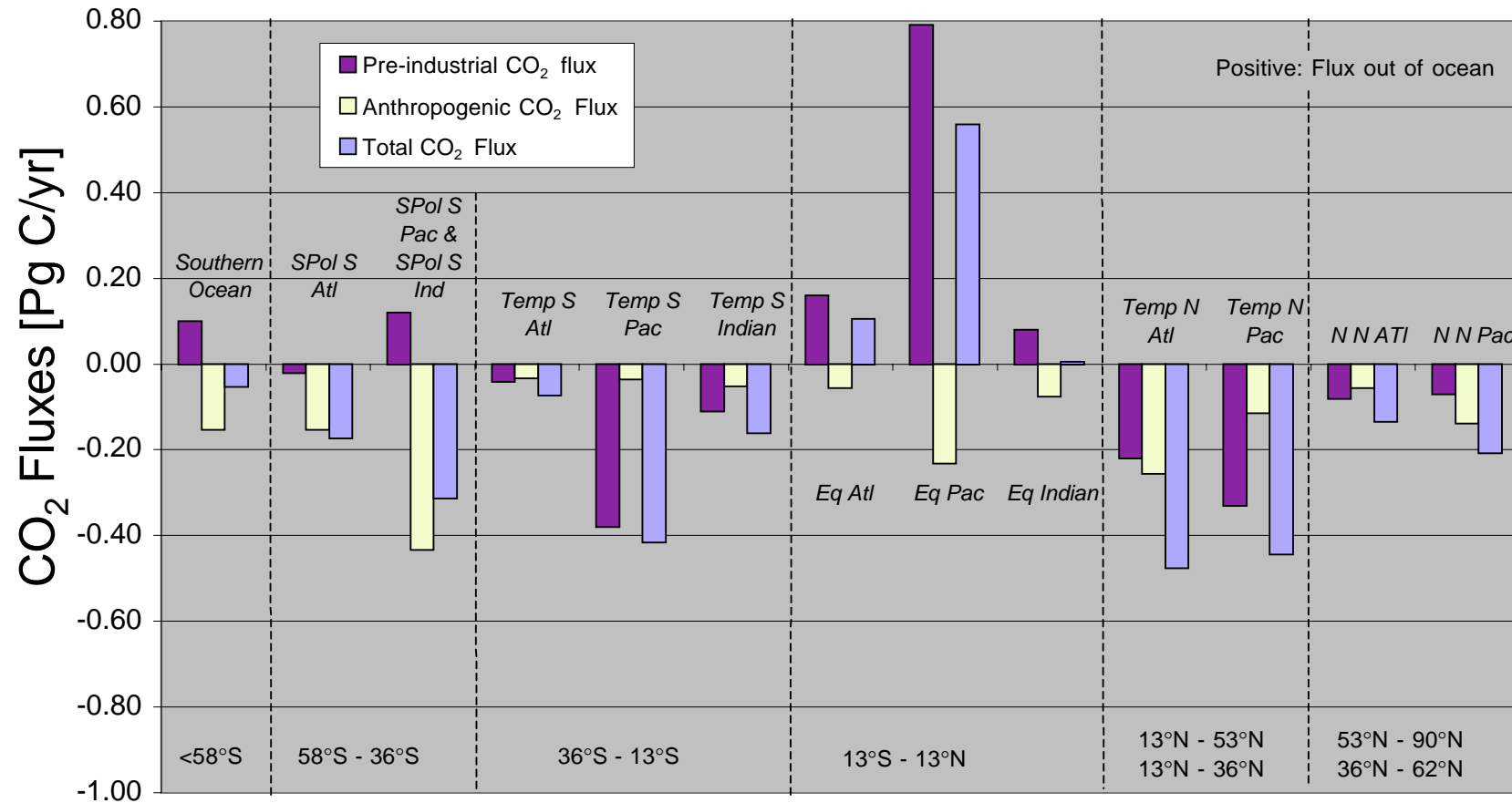


WOCE/JGOFS/OACES SURVEY

## Basis Functions: Color Tracer Distribution



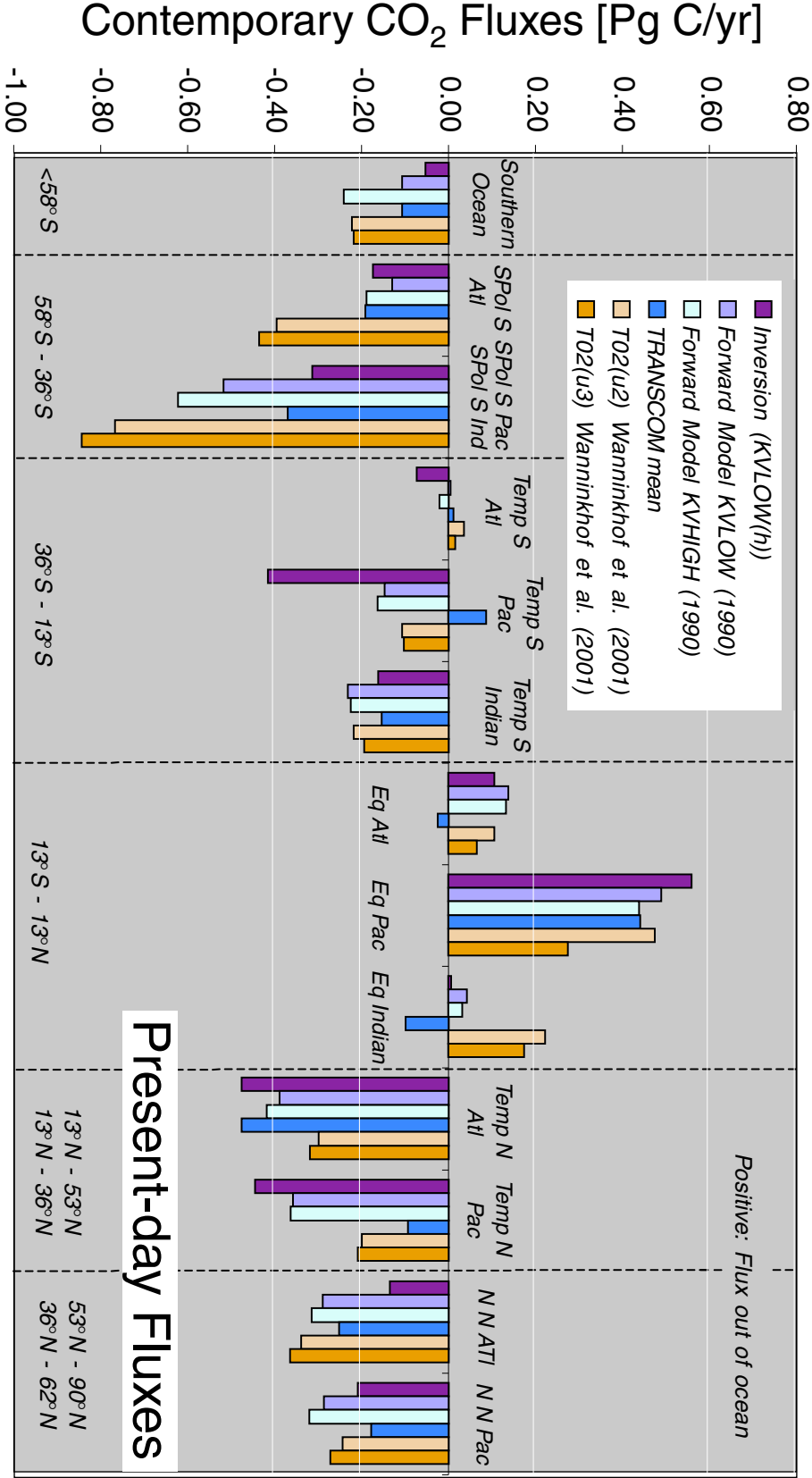
# INVERSE AIR-SEA CO<sub>2</sub>-FLUXES



Anthropogenic CO<sub>2</sub> Flux: 1.8 PgC yr<sup>-1</sup>

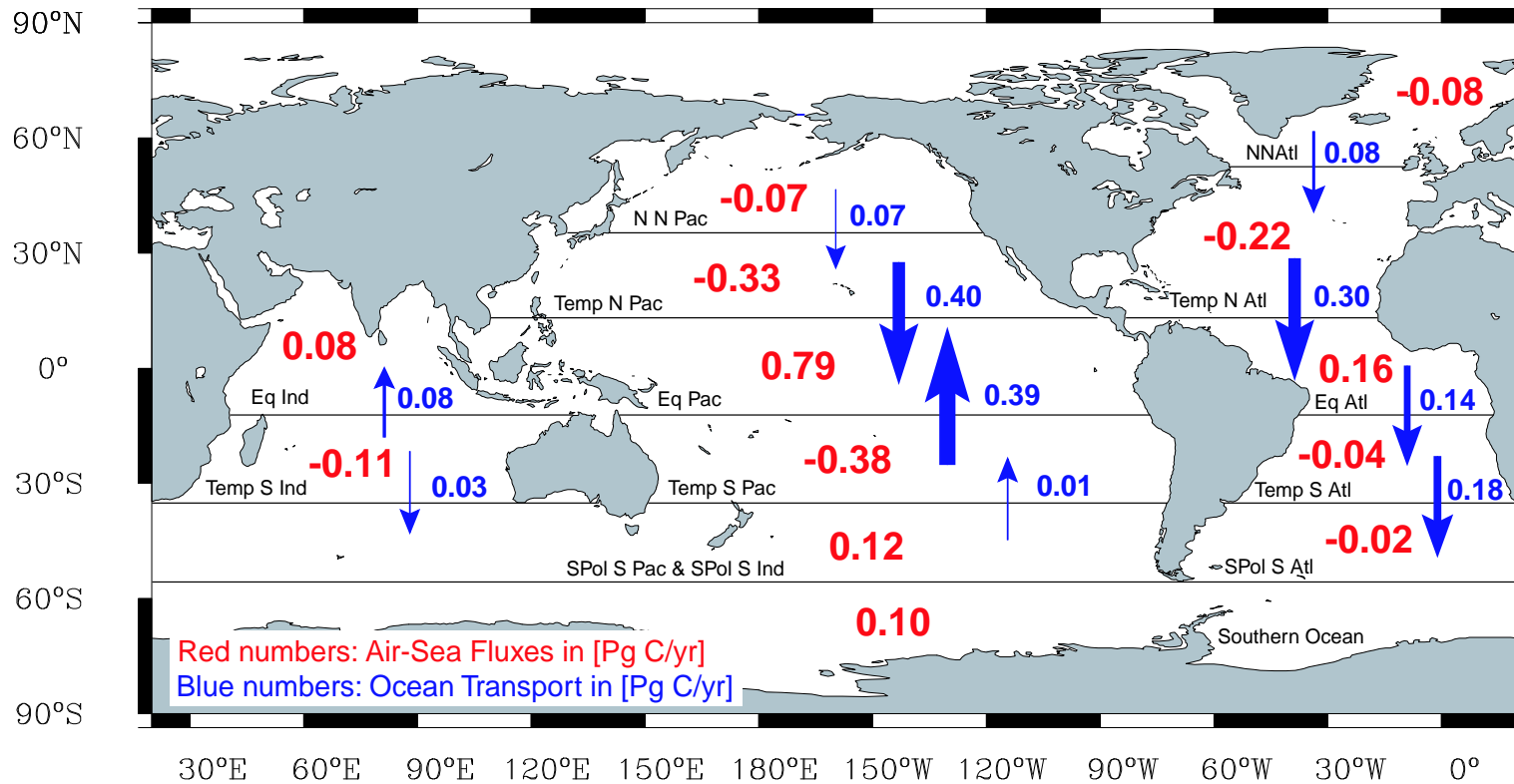
Gloor et al. (submitted),  
Gruber et al. (in prep.)

# PRESENT-DAY AIR-SEA CO<sub>2</sub>-FLUXES (1990)



Gloor et al. (submitted)  
Gruber et al. (in prep.)

# PRE-INDUSTRIAL AIR-SEA FLUXES AND TRANSPORT

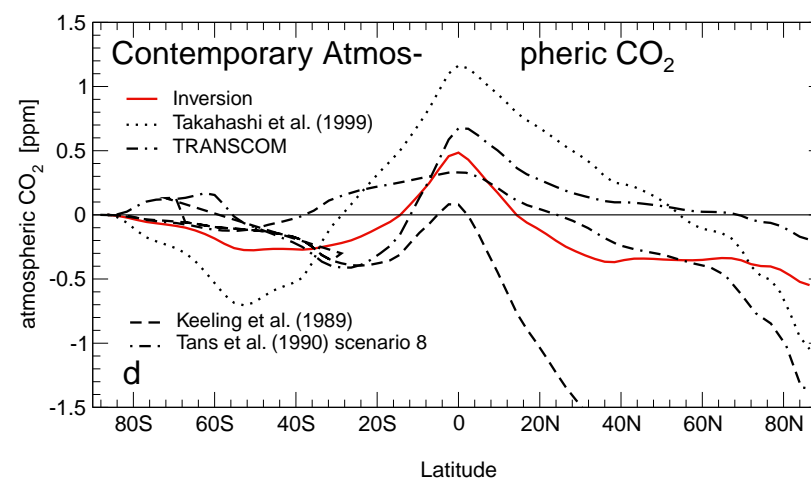
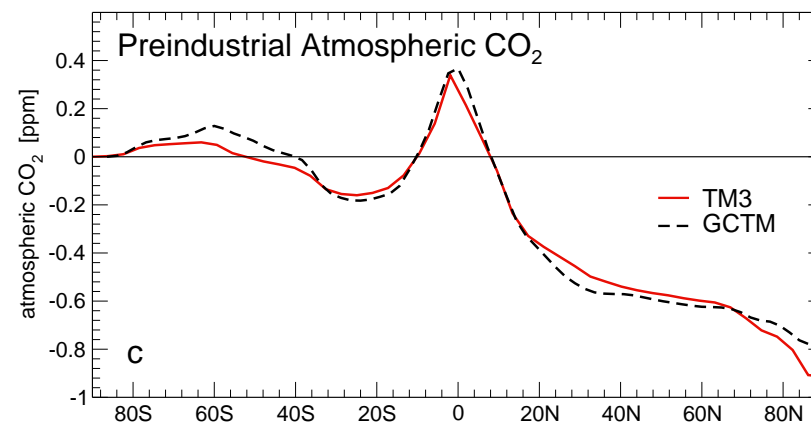
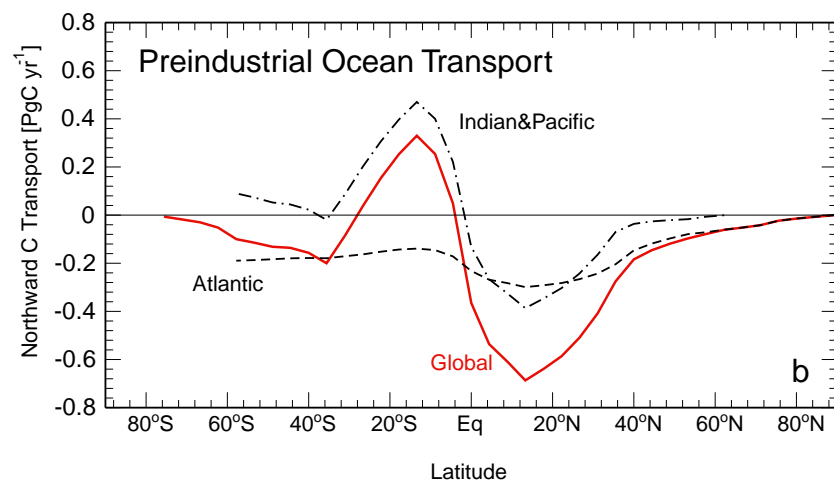
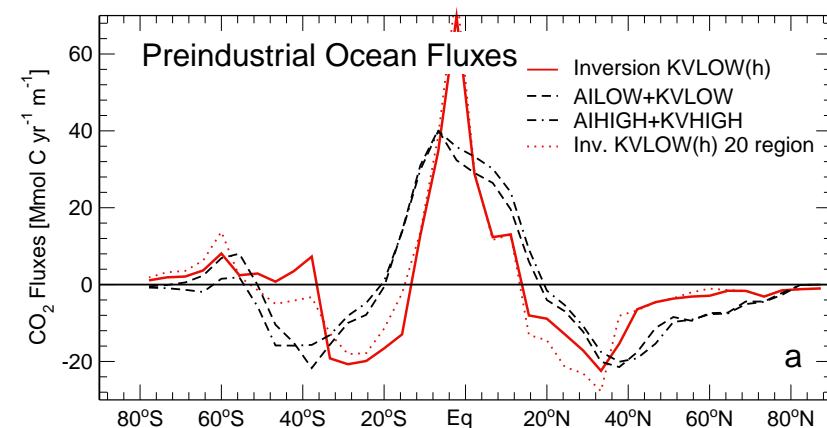


Transport across Equator:  $0.4 \text{ PgC yr}^{-1}$

Transport vanishes at about  $3^\circ\text{S}$

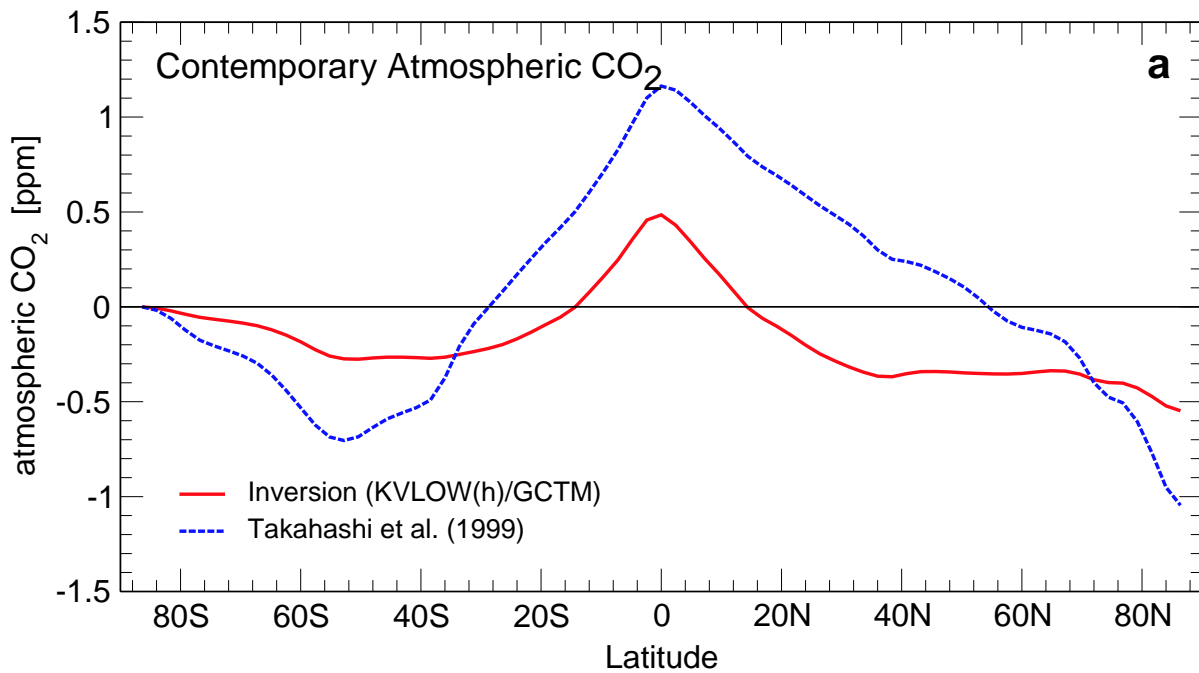


# OCEAN INVERSION

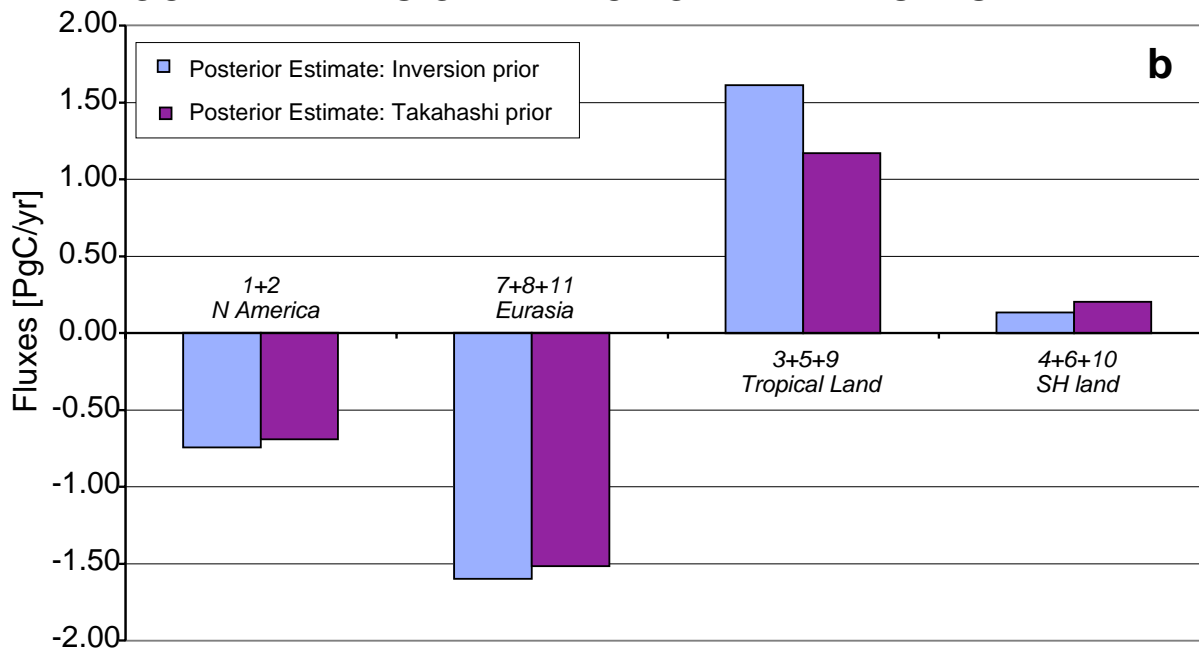


Gloor et al. (submitted)  
 Gruber et al. (in prep.)

## OCEAN INVERSION: ATMOSPHERIC RESPONSE

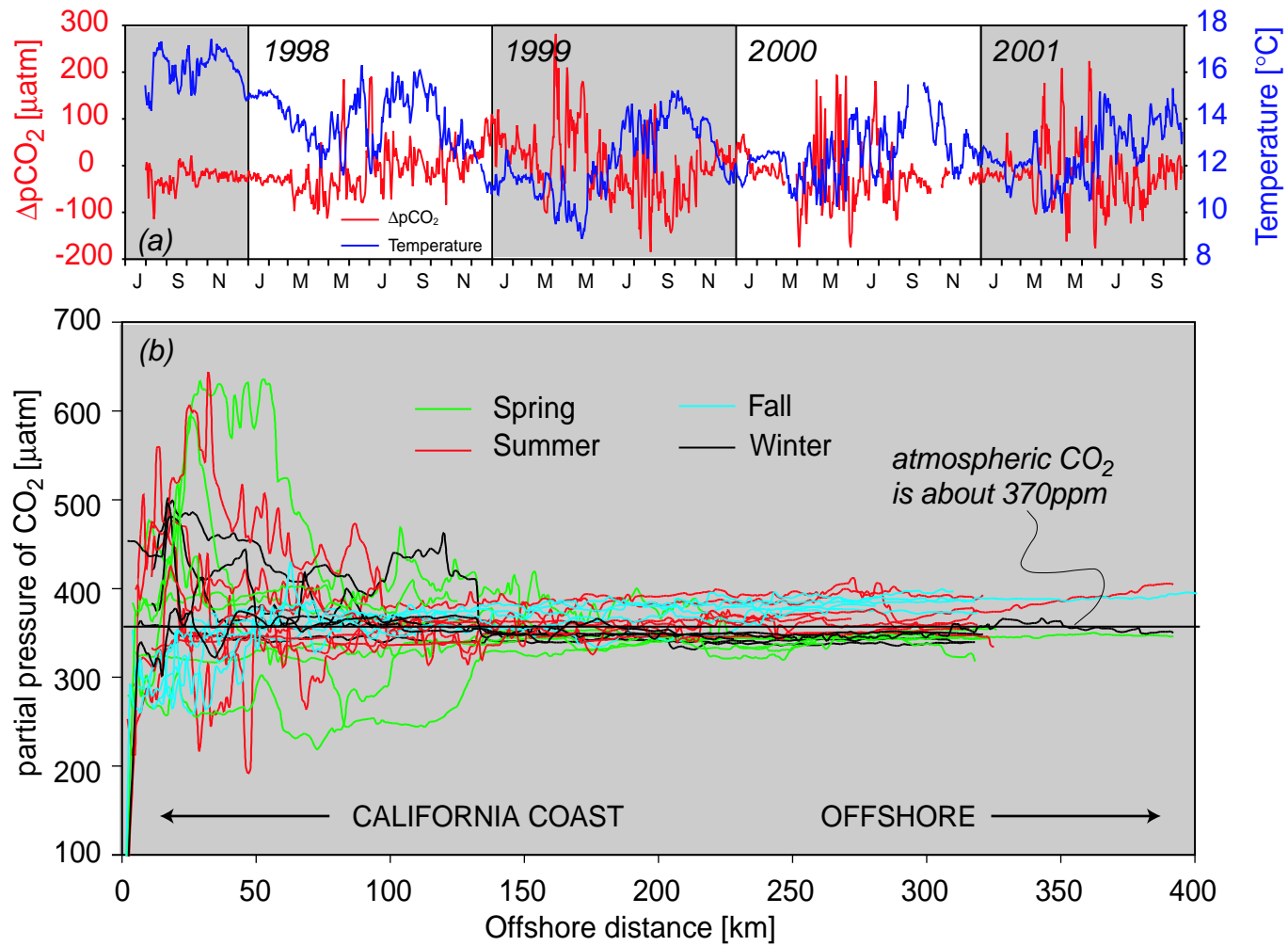


## OCEAN INVERSION: IMPACT ON LAND FLUXES



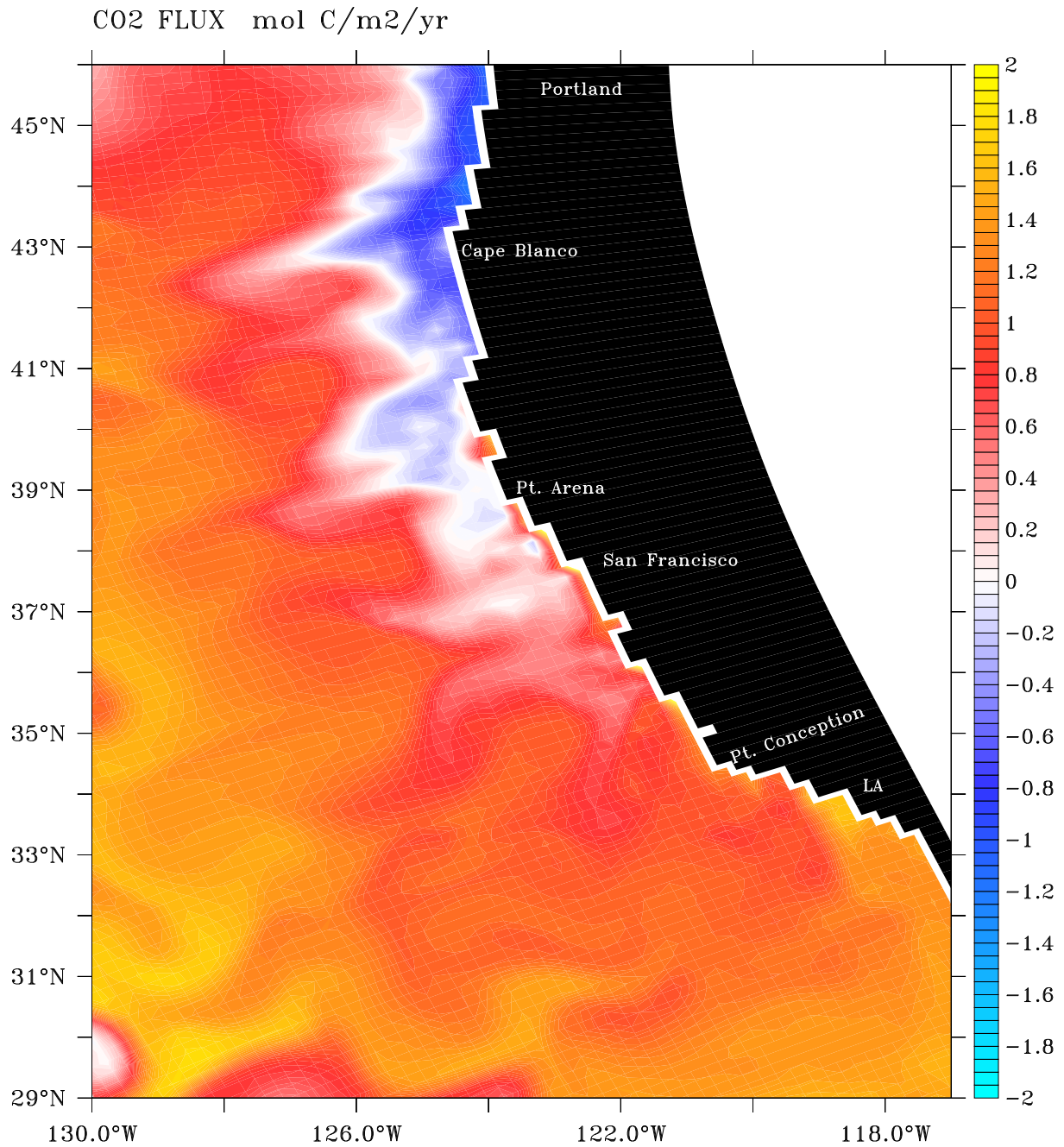
Gruber et al. (in prep.)

## $p\text{CO}_2$ VARIABILITY NEAR MONTEREY BAY



Friederich et al. (in press)  
Chavez et al. (in prep.)

# Regional Ocean Modeling System (ROMS)



*Gruber et al. (in prep.)*

## Summary and Outlook

- Forward and inversely based estimates of the pre-industrial and anthropogenic CO<sub>2</sub> fluxes show overall very similar patterns and magnitudes, which are generally similar to observationally based estimates.
- However, this agreement breaks down in the Southern Hemisphere. In particular, the inversely based estimates indicate a substantially smaller CO<sub>2</sub> uptake in the subpolar regions than indicated by  $\Delta p\text{CO}_2$  based estimates. Atmospheric inversions tend to come to similar conclusions.
- OCMIP forward models and our inverse models find a southward CO<sub>2</sub> transport of the order of 0.4 Pg C yr<sup>-1</sup> across the equator. This is considerably smaller than has been proposed by *Keeling et al.* [1989], and *Broecker and Peng* [1992]. We nevertheless find an interhemispheric gradient in atmospheric CO<sub>2</sub>, but primarily driven by the within hemisphere asymmetry in the fluxes.
- We find that our inversely estimated CO<sub>2</sub> fluxes, when used as priors in an atmospheric CO<sub>2</sub> inversion instead of those by *Takahashi et al.* [1999], lead to a relatively small change in the northern hemisphere terrestrial fluxes, but large changes in the tropical and southern hemisphere land regions.

- Regional ocean modeling advances have made it possible to address also the highly variable CO<sub>2</sub> flux dynamics of the coastal ocean, which might be important for regional atmospheric CO<sub>2</sub> inversions.
- There is large potential in further exploring how inverse techniques can be used to fuse at the same time oceanic and atmospheric data with models.